

UNIVERSITY OF TORONTO  
Faculty of Arts and Science

August 2018 EXAMINATIONS

STA248H1S

Duration - 3 hours

Examination Aids: Scientific Calculator

**STA248H1S**  
**Summer 2018**  
**Final Exam**  
**17/08/2018**  
**Time Limit: 3 hours**

Last Name (Print): \_\_\_\_\_

First Name (Print): \_\_\_\_\_

Student Number: \_\_\_\_\_

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This exam contains 18 pages (including this cover page) and 5 problems. Check to see if any pages are missing. Enter all requested information on the top of this page.

- This is a closed-book exam. You are only allowed to use a scientific calculator and the formulae from the last page of the exam.
- ANOVA stands for ‘Analysis of Variance’;  
MLE stands for ‘Maximum Likelihood Estimator’;  
MSE stands for ‘Mean Squared Error’;
- You are required to show your work on each problem on this exam. Please carry all possible precision through a numerical question, and give your final answer to three (3) decimals, unless they are trailing zeroes or otherwise indicated.
- You may use a benchmark of  $\alpha = 5\%$  for all inference, unless otherwise indicated.

Problem	Points	Score
1	20	
2	25	
3	15	
4	15	
5	25	
Total:	100	

**Additional information and formula:**

$$\Phi^{-1}(0.75) = 0.674, \quad \Phi^{-1}(0.80) = 0.842, \quad \Phi^{-1}(0.85) = 1.036;$$

$$\Phi^{-1}(0.925) = 1.439, \quad \Phi^{-1}(0.95) = 1.645, \quad \Phi^{-1}(0.995) = 2.576.$$

Mean and variance of  $Y \sim \chi^2(n-1)$  are  $n-1$  and  $2(n-1)$ , respectively.

Mean and variance of  $Y \sim \text{Binom}(n, p)$  are  $np$  and  $np(1-p)$ , respectively.

$$Z_d = \frac{\bar{X}_1 - \bar{X}_2 + (\mu_1 - \mu_2)}{\sqrt{\sigma_1^2/n_1 + \sigma_2^2/n_2}}$$

$$S_p = \sqrt{((n_1 - 1)S_1^2 + (n_2 - 1)S_2^2)/(n_1 + n_2 - 2)}$$

$$T = \frac{\bar{X}_1 - \bar{X}_2 + (\mu_1 - \mu_2)}{\sqrt{\sigma_1^2/n_1 + \sigma_2^2/n_2}} \quad T = \frac{\bar{X}_1 - \bar{X}_2 + (\mu_1 - \mu_2)}{\sqrt{S_1^2/n_1 + S_2^2/n_2}}$$

$$F = \frac{MST}{MSE} = \frac{\sum_{i=1}^k n_i (\bar{X}_i - \bar{X})^2 / (k-1)}{\sum_{i=1}^k \sum_{j=1}^{n_i} (X_{ij} - \bar{X}_i)^2 / (N-k)}$$

$$R^2 = \frac{\sum_{i=1}^n (\hat{a} + \hat{b}X_i - \bar{Y})^2}{\sum_{i=1}^n (Y_i - \bar{Y})^2}$$

$$b = \frac{\Sigma(X_i - \bar{X})(Y_i - \bar{Y})}{\Sigma(X_i - \bar{X})^2} = \frac{\Sigma X_i Y_i - n\bar{X}\bar{Y}}{\Sigma X_i^2 - n\bar{X}^2} \quad a = \bar{Y} - b\bar{X}$$

$$\text{Var}(b) = \frac{\sigma^2}{\Sigma(X_i - \bar{X})^2} \quad \text{Var}(a) = \sigma^2 \left( \frac{1}{n} + \frac{\bar{X}^2}{\Sigma(X_i - \bar{X})^2} \right)$$

$$r_{X,Y} = \frac{\Sigma(X_i - \bar{X})(Y_i - \bar{Y})}{\sqrt{\Sigma(X_i - \bar{X})^2 \Sigma(Y_i - \bar{Y})^2}}$$

<b>Z</b>	<b>0.00</b>	<b>0.01</b>	<b>0.02</b>	<b>0.03</b>	<b>0.04</b>	<b>0.05</b>	<b>0.06</b>	<b>0.07</b>	<b>0.08</b>	<b>0.09</b>
<b>0.0</b>	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
<b>0.1</b>	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
<b>0.2</b>	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
<b>0.3</b>	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
<b>0.4</b>	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
<b>0.5</b>	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
<b>0.6</b>	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
<b>0.7</b>	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
<b>0.8</b>	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
<b>0.9</b>	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
<b>1.0</b>	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
<b>1.1</b>	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
<b>1.2</b>	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
<b>1.3</b>	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
<b>1.4</b>	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
<b>1.5</b>	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
<b>1.6</b>	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
<b>1.7</b>	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
<b>1.8</b>	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
<b>1.9</b>	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
<b>2.0</b>	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
<b>2.1</b>	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
<b>2.2</b>	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
<b>2.3</b>	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
<b>2.4</b>	0.9918	0.9920	0.9922	0.9924	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
<b>2.5</b>	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
<b>2.6</b>	0.9953	0.9955	0.9956	0.9957	0.9958	0.9960	0.9961	0.9962	0.9963	0.9964
<b>2.7</b>	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
<b>2.8</b>	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
<b>2.9</b>	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986

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